Pre-processing: spotted DNA microarrays



Terminology

- Target: DNA hybridized to the array, mobile substrate.
- Probe: DNA spotted on the array, aka. spot, immobile substrate.
- Sector: collection of spots printed using the same print-tip (or pin),

aka. print-tip-group, pin-group, spot matrix, grid.

- The terms slide and array are often used to refer to the printed microarray.
- Batch: collection of microarrays with the same probe layout.
- Cy3 = Cyanine 3 = green dye.
- Cy5 = Cyanine 5 = red dye.

Image analysis

 The raw data from a cDNA microarray experiment consist of pairs of image files, 16-bit TIFFs, one for each of the dyes.

 Image analysis is required to extract measures of the red and green fluorescence intensities, R and G, for each spot on the array.

Image analysis

1. Addressing. Estimate location of spot centers.

2. Segmentation. Classify pixels as foreground (signal) or background.

3. Information extraction. For each spot on the array and each dye

- foreground intensities;
- background intensities;
- quality measures.

R and **G** for each spot on the array.



Local background



---- GenePix ---- QuantArray ---- ScanAnalyze

Spot uses Morphological opening

Single-slide data display

- Usually: R vs. G $\log_2 R$ vs. $\log_2 G$.
- Preferred

 $M = \log_2 R - \log_2 G$

- vs. $A = (log_2R + log_2G)/2$.
- An MA-plot amounts to a 45° clockwise rotation of a

 log_2R vs. log_2G plot followed by scaling.

RvG Plot



MvA Plot



Background matters



 $M = \log_2 R - \log_2 G \quad vs. \quad A = (\log_2 R + \log_2 G)/2$

Diagnostic plots

Diagnostics plots of spot statistics

E.g. red and green log-intensities, intensity logratios M, average log-intensities A, spot area.

- Boxplots;
- 2D spatial images;
- Scatter-plots, e.g. MA-plots;
- Density plots.
- **Stratify** plots according to layout parameters, e.g. print-tip-group, plate.

Boxplots by print-tip-group

Swirl 93 array: pre-normalization log-ratio M



MA-plot by print-tip-group

$M = \log_2 R - \log_2 G, A = (\log_2 R + \log_2 G)/2$

Swirl 93 array: pre-normalization log-ratio M





Average log-intensity, A

2D spatial images





Cy5 background intensity



2D spatial images



Intensity log-ratio, M



- After image processing, we have measures of the red and green fluorescence intensities, R and G, for each spot on the array.
- Normalization is needed to ensure that differences in intensities are indeed due to differential expression, and not some printing, hybridization, or scanning artifact.
- Normalization is necessary before any analysis which involves within or between slides comparisons of intensities, e.g., clustering, testing.

- Identify and remove the effects of systematic variation in the measured fluorescence intensities, other than differential expression, for example
 - different labeling efficiencies of the dyes;
 - different amounts of Cy3- and Cy5-labeled mRNA;
 - different scanning parameters;
 - print-tip, spatial, or plate effects, etc.

- The need for normalization can be seen most clearly in self-self hybridizations, where the same mRNA sample is labeled with the Cy3 and Cy5 dyes.
- The imbalance in the red and green intensities is usually not constant across the spots within and between arrays, and can vary according to overall spot intensity, location, plate origin, etc.
- These factors should be considered in the normalization.

Self-self hybridization

$\log_2 R vs. \log_2 G$

M vs. A



 $M = log_2 R - log_2 G$, $A = (log_2 R + log_2 G)/2$

Self-self hybridization

M vs. A



Robust local regression within sectors (print-tip-groups) of intensity log-ratio M on average log-intensity A.

 $M = \log_2 R - \log_2 G, \quad A = (\log_2 R + \log_2 G)/2$

Example of Normalization

 $log_2R/G \leftarrow log_2R/G - L(intensity, sector, ...)$

- Constant normalization: L is constant
- Adaptive normalization: L depends on a number of predictor variables, such as spot intensity A, sector, plate origin.
 - Intensity-dependent normalization.
 - Intensity and sector-dependent normalization.
 - 2D spatial normalization.
 - Other variables: time of printing, plate, etc.
 - Composite normalization. Weighted average of several normalization functions.

2D images of L values

-1

Global median normalization





Global loess 0.56 0.33 normalization 0.11

0.78

-0.11

-0.33

-0.56

- -0.78

-2

Within-print-tipgroup loess normalization







2D images of normalized M-L

Global median normalization





Global loess normalization

- 2

- 1.3

- 0.67

0

- 2.4

- 0.22

-0.33

- 0.89

- -1.4

Within-print-tipgroup loess normalization



irl 93 array: within-print-tip-group loess normalization log-ra



2D spatial - 1.9 - 1.3 normalization 0.78

Boxplots of normalized M-L



Swirl 93 array: within-print-tip-group loess normalization log-ratio



Swirl 93 array: 2D spatial loess normalization log-ratio M

PrintTip

Global loess normalization



Within-print-tipgroup loess normalization





MA-plots of normalized M-L

m - (11) - - (12)

Global median normalization



Swirl 93 array: global median normalization log-ratio M

Swirl 93 array: within-print-tip-group loess normalization log-ratio

10

A

 Σ

Swirl 93 array: global loess normalization log-ratio M

Global loess normalization

Swirl 93 array: 2D spatial loess normalization log-ratio M

Within-print-tipgroup loess



2D spatial normalization

Some References

- Dudoit, Yang, Callow, and Speed: Statistica Sinica (2002)
- Dudoit and Yang (2002) Chap 2 in *The Analysis* of Gene Expression Data
- Yang, Buckley, Dudoit, and Speed: JCGS (2002)
- Kerr and Churchill: Biostatistics (2001)
- Colantuoni, Henry, Zeger, and Pevsner: Bioinformatics (2002)

marray: Pre-processing spotted DNA microarray data

marrayClasses:

- class definitions for cDNA microarray data (MIAME);
- basic methods for manipulating microarray objects: printing, plotting, subsetting, class conversions, etc.

• marrayInput:

- reading in intensity data and textual data describing probes and targets;
- automatic generation of microarray data objects;
- widgets for point & click interface.
- **marrayPlots**: diagnostic plots.
- marrayNorm: robust adaptive location and scale normalization procedures.

Pre-processing: oligonucleotide chips





Probe-pair set



Before Hybridization



More Realistic



Non-specific Hybridization



GeneChip[®] Expression Array Design



Figure 1-3 Expression tiling strategy

Terminology

- Each gene or portion of a gene is represented by 16 to 20 oligonucleotides of 25 base-pairs.
- Probe: an oligonucleotide of 25 base-pairs, i.e., a 25-mer.
- Perfect match (PM): A 25-mer complementary to a reference sequence of interest (e.g., part of a gene).
- Mismatch (MM): same as PM but with a single homomeric base change for the middle (13th) base (transversion purine <-> pyrimidine, G <->C, A <->T).
- Probe-pair: a (PM,MM) pair.
- Probe-pair set: a collection of probe-pairs (11 to 20) related to a common gene or fraction of a gene.
- Affy ID: an identifier for a probe-pair set.
- The purpose of the MM probe design is to measure non-specific binding and background noise.

Why Analyze Probe Level Data?

- Quality control
 - Spatial Effects
 - RNA degradation (Leslie Cope)
- Detection of defective probes
- Transcript sequence "estimates" change
- Ways to reduce to expression measure keep improving

QC

raw values


QC

raw values



log2-transformed values



Statistical Problem

- Each gene is represented by 20 pairs (PM and MM) of probe intensities
- Each array has 8K-20K genes
- Usually there are various arrays
- Obtain measure for each gene on each array: Summarize 20 pairs
- Background correction and normalization are issues

Default until 2002 (MAS 4.0)

• GeneChip® software used Avg.diff

$$Avg.diff = \frac{1}{|\mathsf{A}|} \sum_{j \in \mathsf{A}} (PM_j - MM_j)$$

- with A a set of "suitable" pairs chosen by software.
- Obvious Problems:
 - Many negative expression values
 - No log transform

Why use log?



Current default (MAS 5.0)

• GeneChip[®] new version uses something else

 $signal = TukeyBiweight\{\log(PM_{j} - MM_{j}^{*})\}$

- with MM* a version of MM that is never bigger than PM.
- Ad-hoc background procedure and scale normalization are used.

Can this be improved?



Use Spike-In Experiment



Use Spike-In Experiment



Why background correct?





300

Why normalize?

Density of PM probe intensities for Spike-In chips



Compliments of Ben Bolstad

Why fit statistical models to obtain summaries?



concentration

Example of use of statistical models

- Instead of subtracting MM
- Assume PM = B + S
- To estimate *S*, use expectation: E[S|B+S]
- After normalization, assume: $log_2S_{ij} = E_i + P_j + \varepsilon_{ij}$
- Estimate E_i using robust procedure
- We call this procedure RMA
- Does it make a difference?

MAS 5.0



Perfect



А

RMA



А

Some References

- Li and Wong: PNAS (2001)
- Irizarry et al: Biostatistics (2003)
- Irizarry et al: NAR (2003)
- Bolstad et al: Bioinformatics (2003)

Differential gene expression



Differential gene expression

- Identify genes whose expression levels are **associated** with a response or covariate of interest
 - clinical outcome such as survival, response to treatment, tumor class;
 - covariate such as treatment, dose, time.
- Estimation: In a statistical framework, assigning a score can be viewed as estimating an effects of interest (e.g. difference in means, slope, interaction). We can also take the **variability** of these estimates into account.
- **Testing**: In a statistical framework, **deciding on a cut-off** can be viewed as an assessment of the statistical **significance** of the observed associations.

Example: Two populations

A common problem is to find genes that are differentially expressed in two populations.

Many method papers appear in both statistical and molecular biology literature.

The proposed scores range from:

- ad-hoc summaries of fold-change,
- variantes on the t-test,
- and posterior means obtained from Bayesian or empircal Bayes methods.

What's the difference? Mainly the way in which the variation within population is incorporated

Should we consider variability of estimate?



Should we consider variability of estimate?



Should we consider variability of estimate?





Some Examples

Notation: log expression, population i, gene j, array k:

 $Y_{jk}(i), j = 1, \dots, J, k = 1, \dots, K = K_1 + K_2, i = 1, 2.$

- log fold-change: $\bar{Y}_{j(2)} \bar{Y}_{j(1)}$.
- t-statistic: $\frac{\bar{Y}_{j(2)} \bar{Y}_{j(1)}}{s_j}$
- SAM shrunken-t: $\frac{\bar{Y}_{j(2)} \bar{Y}_{j(1)}}{s_j + s_0}$.
- Wilcoxon rank-sum

• Bayesian (e.g., Baldi and Long):
$$\frac{\bar{Y}_{j(2)} - \bar{Y}_{j(1)}}{\sqrt{(1-w)s_j^2 + ws_0^2}}$$
.

Does it make a difference?

• Data:

Spike-in data from Affymetrix, 16 spike-in genes with known spikein concentrations

- Properties of "good method"
 - rank truely differentially expressed genes higher than non-differential ones \longrightarrow sensitivity, specificity ROC curves





Hypothesis testing

Once you have a score for each gene, how do you decide on a cut-off? p-values are popular. Are they appropriate?

- Test for each gene **null hypothesis**: no differential expression.
 - H_g : the expression level of gene g
 - is not associated with the covariate or response.

Two types of errors can be committed

• Type I error or false positive

say that a gene is differentially expressed when it is not, i.e., reject a *true null* hypothesis.

• **Type II error** or **false negative** fail to identify a truly differentially expressed gene, i.e., fail to reject a *false null* hypothesis.

Multiple hypothesis testing

- Large multiplicity problem: thousands of hypotheses are tested simultaneously!
 - Increased chance of false positives.
 - E.g. chance of at least one *p*-value $< \alpha$ for *G* independent tests is $1 - (1 - \alpha)^G$ and converges to one as *G* increases. For G = 1,000 and $\alpha = 0.01$, this chance is 0.9999568!
 - Individual p-values of 0.01 no longer correspond to significant findings.
- Need to **adjust for multiple testing** when assessing the statistical significance of the observed associations.

Multiple hypothesis testing

- Define an appropriate **Type I error** or **false positive rate**.
- Develop multiple testing procedures that
 - provide **strong control** of this error rate,
 - are **powerful** (few false negatives),
 - take into account the joint distribution of the test statistics.
- Report adjusted *p*-values for each gene which reflect the overall Type I error rate for the experiment.
- **Resampling** methods are useful tools to deal with the unknown joint distribution of the test statistics.

Multiple hypothesis testing



From Benjamini & Hochberg (1995).

Three Examples

FWER(Family-Wise Error Rate)

Probability of including at least one non-differentially expressed genes into your list: p(V > 0)

False discovery rate (FDR). The FDR of Benjamini & Hochberg (1995) is the expected proportion of Type I errors among the rejected hypotheses, i.e.,

FDR = E(Q),

$$Q \equiv \begin{cases} V/R, & \text{if } R > 0, \\ 0, & \text{if } R = 0. \end{cases}$$

pFDR. Expected proportion of false discoveries among the genes in your list conditioning on "at least one gene is included in the differential list": E(Q|R > 0)

Does it make a difference?

• Data:

Spike-in data from Affymetrix, 14 spike-in genes with known concentrations

• Properties of "good method": reported error rate close to true error rate

$$\log\left(\frac{\text{predicted error rate}}{\text{observed error rate}}\right) \approx 0$$

Log ratio of predicted and observed error rates



Demo

- We will demonstrate how to go from a probel level data from two samples hybridized to six Affymetrix arrays to a list of *candidate genes*
- Bioconductor packages used:
 - affy: Preprocessing probe level data
 - **Biobase**: organizes expression level data
 - **multtest**: functions for multiple testing
Affymetrix files

- Main software from Affymetrix company, *MicroArray Suite - MAS*, now version 5.
- **DAT** file: Image file, ~10^7 pixels, ~50 MB.
- **CEL** file: Cell intensity file, probe level PM and MM values.
- CDF file: Chip Description File. Describes which probes go in which probe sets and the location of probe-pair sets (genes, gene fragments, ESTs).

affy: Pre-processing Affymetrix data

- Class definitions for probe-level data: AffyBatch, ProbSet, Cdf, Cel.
- Basic methods for manipulating microarray objects: printing, plotting, subsetting.
- Functions and widgets for data input from CEL and CDF files, and automatic generation of microarray data objects.
- Diagnostic plots: 2D spatial images, density plots, boxplots, MA-plots, etc.

affy classes: AffyBatch

Probe-level intensity data for a batch of arrays (same CDF)



CDF data packages

- Data packages containing necessary CDF information are available at <u>www.bioconductor.org</u>.
- Packages contain environment objects, which provide mappings between AffyIDs and matrices of probe locations,

rows \rightarrow probe-pairs, columns \rightarrow PM, MM (e.g., 20X2 matrix for hu6800).

- cdfName slot of AffyBatch.
- HGU95Av2 and HGU133A provided in affy package.

Expression meassures: expresso













Acknowledgements

Bioconductor core team

- Ben Bolstad, Biostatistics, UC Berkeley
- Vincent Carey, Biostatistics, Harvard
- Francois Collin, GeneLogic
- Leslie Cope, JHU
- Laurent Gautier, Technical University of Denmark, Denmark
- Yongchao Ge, Statistics, UC Berkeley
- Robert Gentleman, Biostatistics, Harvard
- Jeff Gentry, Dana-Farber Cancer Institute
- John Ngai Lab, MCB, UC Berkeley
- Juliet Shaffer, Statistics, UC Berkeley
- Terry Speed, Statistics, UC Berkeley
- Zhijin Wu, Biostatistics, JHU
- Yee Hwa (Jean) Yang, Biostatistics, UCSF
- Jianhua (John) Zhang, Dana-Farber Cancer Institute
- Spike-in and dilution datasets:
 - Gene Brown's group, Wyeth/Genetics Institute
 - Uwe Scherf's group, Genomics Research & Development, GeneLogic.
- **GeneLogic** and **Affymetrix** for permission to use their data.

Supplemental Slides

Diagnostic plots

- See demo(affy).
- Diagnostic plots of probe-level intensities, PM and MM.
 - image: 2D spatial color images of log intensities (AffyBatch, Cel).
 - boxplot: boxplots of log intensities (AffyBatch).
 - mva.pairs: scatter-plots with fitted curves (apply exprs, pm, or mm to AffyBatch object).
 - hist: density plots of log intensities (AffyBatch).

image

read from file: HIVControl4A.CEL.gz



read from file: HIVControl4B.CEL.gz

1.0

0.8

0.6

0.4

0.2

0.0

0.0

1.0 0.8 0.6 0.4 0.2 0.0 Т 0.2 0.4 0.6 0.8 1.0 0.0 0.2 0.4 0.6 0.8

read from file: HIVControl4B.CEL.gz

1.0

hist



hist(Dilution,col=1:4,type="l",lty=1,lwd=3)



Small part of dilution study



boxplot(Dilution,col=1:4)

mva.pairs



Expression measures

- **expresso**: Choice of common methods for
 - background correction: bgcorrect.methods
 - normalization: normalize.AffyBatch.methods
 - probe specific corrections: pmcorrect.methods
 - expression measures: express.summary.stat.methods.
- rma: Fast implementation of RMA (Irizarry et al., 2003): model-based background correction, quantile normalization, median polish expression measures.
- **express**: Implementing your own method for computing expression measures.
- normalize: Normalization procedures in normalize.AffyBatch.methods Or normalize.methods (object).

Probe sequence analysis

- Examine probe intensity based on location relative to 5' end of RNA sequence of interest.
- Expect probe intensities to be lower at 5' end compared to 3' of mRNA.
- E.g.

deg<-AffyRNAdeg(Dilution)</pre>

plotAffyRNAdeg(deg)

multtest package

- Multiple testing procedures for controlling
 - Family-Wise Error Rate FWER: Bonferroni, Holm (1979), Hochberg (1986), Westfall & Young (1993) maxT and minP;
 - False Discovery Rate FDR: Benjamini & Hochberg (1995), Benjamini & Yekutieli (2001).
- Tests based on t- or F-statistics for one- and two-factor designs.
- Permutation procedures for estimating adjusted pvalues.
- Fast permutation algorithm for minP adjusted p-values.
- Documentation: tutorial on multiple testing.

marrayLayout class

Array layout parameters



Total number of spots

Dimensions of grid matrix

Dimensions of spot matrices

Current subset of spots

Plate IDs for each spot

Control status labels for each spot

Any notes

marrayRaw class

Pre-normalization intensity data for a batch of arrays



marrayNorm class

Post-normalization intensity data for a batch of arrays



marrayInput package

- marrayInput provides functions for reading microarray data into R and creating microarray objects of class marrayLayout, marrayInfo, and marrayRaw.
- Input
 - Image quantitation data, i.e., output files from image analysis software.

E.g. .gpr for GenePix, .spot for Spot.

- Textual description of probe sequences and target samples.
 - E.g. gal files, god lists.

marrayInput package

 Widgets for graphical user interface

widget.marrayLayout,

widget.marrayInfo,

widget.marrayRaw.

🥖 MarrayRaw builder			
Files			
Name of the marrayRaw object:			
swir			
Foreground and background intensities			
Green Foreground Gmean	Green Background m	orphG	
Red Foreground Rmean	Red Background m	orphR	
Weights			
Layout:			
swirl.layout		Browse	
Target Information:			
swirl.samples		Browse	
Gene Information:			
swirl.gnames		Browse	
Notes:			
Layout Target Genes B	uild Quit		

marrayPlots package

- See demo (marrayPlots).
- Diagnostic plots of spot statistics.
 - E.g. red and green log intensities, intensity log ratios M, average log intensities A, spot area.
 - maImage: 2D spatial color images.
 - maBoxplot: boxplots.
 - maPlot: scatter-plots with fitted curves and text highlighted.
- Stratify plots according to layout parameters such as print-tip-group, plate.
 E.g. MA-plots with loess fits by print-tipgroup.

marrayNorm package

- maNormMain: main normalization function, allows robust adaptive location and scale normalization for a batch of arrays
 - intensity or A-dependent location normalization (maNormLoess);
 - 2D spatial location normalization (maNorm2D);
 - median location normalization (maNormMed);
 - scale normalization using MAD (maNormMAD);
 - composite normalization;
 - your own normalization function.
- maNorm: simple wrapper function.
 maNormScale: simple wrapper function for scale normalization.

marrayTools package

- The marrayTools package provides additional functions for handling two-color spotted microarray data (see devel. version).
- The **spotTools** and **gpTools** functions start from Spot and GenePix image analysis output files, respectively, and automatically
 - read in these data into R,
 - perform standard normalization (within print-tipgroup loess),
 - create a directory with a standard set of diagnostic plots (jpeg format), excel files of quality measures, and tab delimited files of normalized log ratios M and average log intensities A.

swirl dataset

- Microrrays:
 - 8,448 probes (768 controls);
 - 4 x 4 grid matrix;
 - 22 x 24 spot matrices.
- 4 hybridizations: swirl mutant and wild type mRNA.
- Data stored in object of class marrayRaw: data(swirl).
- > maInfo(maTargets(swirl))[,3:4]

experiment Cy3 experiment Cy5

1	swirl	wild type
2	wild type	swirl
3	swirl	wild type
4	wild type	swirl

Scale normalization

- For print-tip-group scale normalization, assume all print-tip-groups have the same spread in M.
- Denote *true* and *observed* log-ratio by μ_{ij} and M_{ij} , resp., where $M_{ij} = a_i \mu_{ij}$, and i indexes print-tip-groups and j spots. Robust estimate of a_i is

$$\hat{a}_{i} = \frac{MAD_{i}}{\sqrt[I]{\prod_{i=1}^{I} MAD_{i}}}$$

where MAD_i is MAD of M_{ij} in print-tip-group i.

• Similarly for between-slides scale normalization.

Microarray sample pool



MSP Rank invariant Housekeeping Tubulin, GAPDH

MA-plot by print-tip-group maPlot $M = log_2R - log_2G$, $A = (log_2R + log_2G)/2$

Swirl 93 array: pre-normalization log-ratio M

Intensity log ratio, M



Average log intensity, A